

University of Bahrain

College of Information Technology

Department of Computer Engineering

Experiment 3

**Prepared By**

**Name : Ali Redha Ali**

**ID: 20195330**

**Sec: 01**

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**Introduction to Fourier transform**

**Objective:**

1. Introducing the Fourier transformation

2.Introduction to DFT and FFT

**Introduction:**

In this will lab we will learn how to do Fourier transformation in MATLAB

**Procedure**

Part One: Fourier series

The Fourier series of the Square Wave

A close-up of a calculator

Description automatically generated with low confidenceLet the function sq(t) be denoted by

The Fourier series associated with this function is

Company name

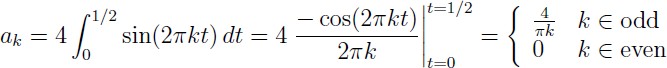
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The Fourier coefficients of this 1-periodic function are given by

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Because sq(t) is odd, it is clear that bk = 0 for all k ≥ 0. From symmetry it is clear that:



Thus, we find that the Fourier series associated with sq(t) is

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A Quick Check

Before proceeding to analyze the series we have found, it behooves us to check that the calculations were performed correctly. For a 1-periodic function like sq(t), Parseval's equation states that

In our case this means that

A close-up of a calculator

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We can check that this sum is correct using MATLAB. One way to perform a quick check is to give MATLAB the commands

L = [1:2:10001];

(8/pi^2) \* sum(1./L.^2)

MATLAB responds with ans =

1.0000

Which is an indication that we may have performed all of the calculations correctly.

A second way to have MATLAB check this computation is to give MATLAB the commands

syms k

(sym('8')/sym('pi')^2) \* symsum(1/(2\*k+1)^2,k,0,Inf)

MATLAB responds to these commands with ans =

1

Indicating that the series does, indeed, sum to 1.

Seeing" the Sum

It is not difficult to have MATLAB calculate the Fourier series and display

its values. Conisder the following code:

t = [-500:500] \* 0.001;

total = zeros(size(t));

for k = 1 : 2 : 101

total = total + (4/pi) \* sin(2\*pi\*k\*t) / k;

end

plot(t,total)

This code denotes a "time" vector, t, with 1001 elements. It then defines a vector to hold the sum, total, and proceeds to sum the first 51 terms in the Fourier series. The code causes MATLAB to produce the plot shown in

Graphical user interface, chart

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Figure 5.1: Summing the Fourier series. The "ringing" associated with Gibb's Phenomenon is clearly visible.

The Experiment

Let

saw(t) = t

for -1/2 < t ≤1/2 and continue saw(t) periodically outside of this region.

1. Calculate the Fourier coefficients associated with saw(t).

2. Check Parseval's equation for saw(t) both numerically and symbolically.

3. Sum the first 3 terms in the Fourier series and plot the Fourier series as a function of time.

4. Sum the first 10 terms in the Fourier series and plot the Fourier series as a function of time.

5. Sum the first 50 terms in the Fourier series and plot the Fourier series as a function of time.

When summing the Fourier series, make sure that the time samples you take are sufficiently closely spaced that you clearly see Gibb's phenomenon.

Part 2: DFT and FFT

Introduction

DFTs with a million points are common in many applications. Modern signal and image processing applications would be impossible without an efficient method for computing the DFT.

Direct application of the definition of the DFT (see [Discrete Fourier Transform (DFT))](http://www.mathworks.com/help/matlab/math/discrete-fourier-transform-dft.html) to a data vector of

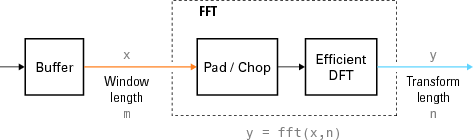
length *n*requires *n* multiplications and *n* additions—a total of 2*n*2 floating-point operations. This does not include the generation of the powers of the complex *n*th root of unity *ω*. To compute a million-point DFT, a computer capable of doing one multiplication and addition every microsecond requires a million seconds, or about 11.5 days.

*Fast Fourier Transform (FFT)* algorithms have computational complexity *O*(*n* log *n*) instead of *O*(*n*2). If *n* is a power of 2, a one-dimensional FFT of length *n* requires less than 3*n* log2 *n* floating-point operations (times a proportionality constant). For *n* = 220, that is a factor of almost 35,000 faster than 2*n*2.

The MATLAB® functions [fft,](http://www.mathworks.com/help/matlab/ref/fft.html) [fft2,](http://www.mathworks.com/help/matlab/ref/fft2.html) and [fftn](http://www.mathworks.com/help/matlab/ref/fftn.html) (and their inverses [ifft,](http://www.mathworks.com/help/matlab/ref/ifft.html) [ifft2,](http://www.mathworks.com/help/matlab/ref/ifft2.html) and [ifftn,](http://www.mathworks.com/help/matlab/ref/ifftn.html) respectively) all

use fast Fourier transform algorithms to compute the DFT.

When using FFT algorithms, a distinction is made between the *window length* and the *transform length*. The window length is the length of the input data vector. It is determined by, for example, the size of an external buffer. The transform length is the length of the output, the computed DFT. An FFT algorithm pads or chops the input to achieve the desired transform length. The following figure illustrates the two lengths.



The execution time of an FFT algorithm depends on the transform length. It is fastest when the transform length is a power of two, and almost as fast when the transform length has only small prime factors. It is typically slower for transform lengths that are prime or have large prime factors. Time differences, however, are reduced to insignificance by modern FFT algorithms such as those used in MATLAB. Adjusting the transform length for efficiency is usually unnecessary in practice.

**Report**

**1-** Consider the following data x with two component frequencies of differing amplitude and phase buried in noise with the following parameters:

a- Sampling frequency = 200hz

b- 20 second samples

c- 20 and 40 hz components

d- Gaussian noise

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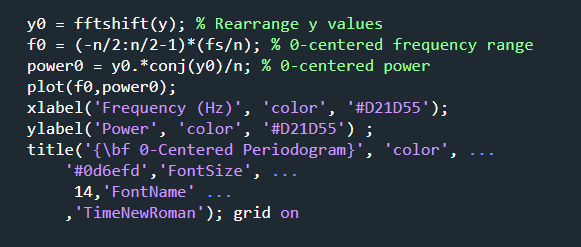
**2- Use FFT to compute DFT y and its power**

**3- Plot the frequency and power**

Chart

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**4- Rearrange the output from fft to produce 0-centered periodogram**



**5- Create and plot the phase**

Chart

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**Conclusion:**

In this lab I learned a lot of things which are

* How to implement signal function in MATLAB
* How to use stem function in MATLAB
* How to use convolution in MATLAB